

Methodological note (Flash6): Regression estimation of average annual percentage reduction in deaths from a time series of number of deaths

The average yearly reduction can be calculated from any two years figures if assuming a uniform annual percentage reduction over the period considered as follows:

$$P(A) = 1 - (Y_{t_2}/Y_{t_1})^{1/(t_2-t_1)} \times 100\%$$

where Y_t stands for the number of deaths in any year t and $P(A)$ stands for the average yearly reduction over the period considered.

Example:

(halving the number of deaths in the EU)

$Y_{t_1} = 50,000$ (1), $Y_{t_2} = 25,000$ (0.5) over the period 2001-2010 ($2010-2001 = (t_2-t_1) = 9$)

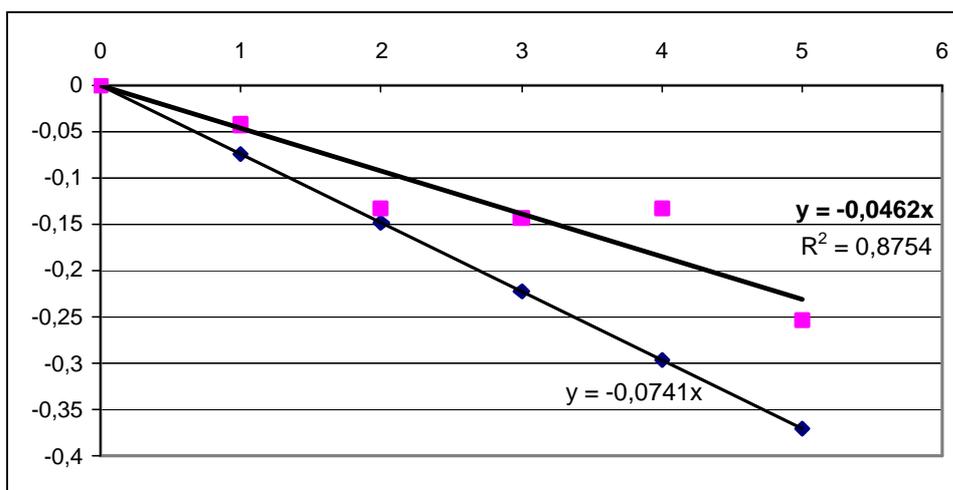
$$P(A) = 1 - (0.5)^{1/9} = 0.07413 = 7.4\% \text{ (rounded for practical purposes)}$$

Halving over 9 years requires a uniform annual percentage reduction of 7.413 per cent (7.4 per cent for practical purposes).

For estimating the average annual percentage reduction in deaths achieved by a country between year 0 and year N (e.g. between 2001 and 2006 with $N = 5$ for comparison with the required 7.4 per cent) one should make use of the whole time series of numbers of deaths, not just the numbers in years 0 and N .

Let the average reduction per year as a percentage of the previous year be p . If Y_n is the number of deaths in year n , then we wish to fit a model $Y_n = Y_0(1 - p/100)^n$.

This is equivalent to $\ln(Y_n/Y_0) = n \ln(1 - p/100)$ so if we fit $\ln(Y_n/Y_0) = an$ by linear regression, then a is the estimate of $\ln(1 - p/100)$ and p is estimated by $100(1 - e^a)$.



In this figure illustrating the use of the method and constructed for Finland, the function $\ln(Y_n/Y_0) = an$ corresponds to the function $y=ax$. The targeted reduction curve is shown together with the fitted (linear regression) line.